

Write neat, concise, and accurate solutions to each problem. No calculators are allowed.

1. Find the limit of the sequence $\left\{ \frac{3n-1}{\sqrt{2n^2-n+4}} \right\}$.
2. Find the limit of the sequence $\left\{ \left(\frac{2n+1}{2n} \right)^n \right\}$.
3. Find the limit of the sequence $\left\{ 4\sqrt[n]{7} - \sqrt[n]{n^2} \right\}$.
4. Give an example of a bounded sequence that does not converge.
5. Give an example of a decreasing sequence that does not converge.
6. Give an example of a convergent sequence that is not monotone.
7. Give an example of a divergent series whose terms converge to 0.
8. Find the sum of the series $8 - 6 + \frac{9}{2} - \frac{27}{8} + \dots$.
9. Find the sum of the series $\sum_{k=1}^{\infty} \frac{3^{k-1}}{5^{2k}}$.
10. Consider the sequence $\{a_n\}$ defined by $a_1 = 1$ and $a_{n+1} = 7 - \frac{3}{a_n}$ for each $n \geq 1$. Use mathematical induction to prove that $\{a_n\}$ is an increasing sequence.
11. Determine whether or not the series $\sum_{k=2}^{\infty} \frac{1}{\ln k}$ converges.
12. Determine whether or not the series $\sum_{k=1}^{\infty} \frac{2k-1}{k^3+5k-2}$ converges.
13. Classify the series $\sum_{k=1}^{\infty} \frac{(-1)^{k+1}}{4k+1}$ as absolutely convergent, conditionally convergent, or divergent.
14. Determine whether or not the series $\sum_{k=1}^{\infty} \frac{(2k)!}{7^k(k!)^2}$ converges.
15. Find a power series centered at 0 that represents the function $f(x) = \frac{x}{1-x^2}$.
16. Find the interval of convergence for the power series $\sum_{k=0}^{\infty} \frac{(-1)^{k+1}}{3^k(5k+2)} (x-4)^k$.