

Extra Examples, 11.2

1. Does the series converge or diverge?

(a)
$$\sum \frac{k(k+2)}{(k+3)^2}$$

(b)
$$\sum_{n=1}^{\infty} \frac{5}{n^2}$$

(c)
$$\sum_{n=2}^{\infty} \frac{1+3^n}{5^n}$$

2. What's wrong?

$$\begin{aligned}0 &= 0 + 0 + 0 + 0 + \dots \\ &= (1 - 1) + (1 - 1) + (1 - 1) + \dots \\ &= 1 - 1 + 1 - 1 + 1 - 1 + \dots \\ &= 1 + (-1 + 1) + (-1 + 1) + (-1 + 1) + \dots \\ &= 1 + 0 + 0 + 0 + 0 + \dots\end{aligned}$$

Therefore, $0 = 1$.