

- 5.3.1 Use quadratic reciprocity plus theorem 5.3. The first is  $-1$ , the second is  $1$ .
- 5.3.2 You can use theorem 5.8, but this is easy enough that you don't need it. Remember theorem 5.5.
- 5.3.9 Use the example at the bottom of page 106 for  $q = 3$ . For the last part, show that  $(-3/p) = 1$  for infinitely many primes  $p$ . Start in the usual way, by assuming that only primes  $p_1$  through  $p_n$  work; use theorem 5.1 to get a contradiction.
- 6.3.4 If  $x = m/n$ , find an explicit formula for  $a_1$ . Use induction on  $m$  to show the expansion for  $x$  is finite.

For part b, show that the sequence  $\{b_i\}$  is an infinite sequence with the property described in part a. The trickiest bit is showing that  $b_i = 2^{3^k} + 1$  has the defining property.

- 6.4.4 Start by taking the derivative of  $x/\ln(x)$  to get some help with the antiderivative of  $1/\ln(t)$ . You won't be able to do the anti-derivative explicitly, but you can get to  $x/\ln(x) + A$ , and then show  $A = O(x/\ln^2(x))$ .