## SAMPLE EXAM 2

- 1. Let  $f(x,y) = \ln(x^2 + y^2)$ . Compute the partial derivatives  $f_x$ ,  $f_y$ ,  $f_{xx}$ ,  $f_{yy}$ ,  $f_{xy}$ ,  $f_{yx}$ .
- 2. Describe the level curves of  $f(x,y) = \frac{x^2}{9} + \frac{y^2}{16}$ .
- 3. Find an equation for the tangent plane to  $z = e^y \ln x$  at (1, 3, 0).
- 4. Use the "two-variable" version of the chain rule to compute g'(t) if  $g(t) = \ln(x^2 + y^2)$ ,  $x = t^2$ , and  $y = \cos t$ . Your answer should contain all of x, y, and t.
- 5. Suppose z = f(x, y). Describe the significance of both the length and the direction of  $\nabla f$  at a point  $(x_0, y_0)$ .
- 6. Find the directional derivative of  $f(x,y) = x^2y^3 + xy$  at the point (-1,2) in the direction indicated by the vector (3,-2).
- 7. Find the directional derivative of  $f(x, y, z) = x^2yz^3 + xy z$  at the point (1, 1, 1) in the direction indicated by the vector (1, 2, 3).
- 8. Find an equation for the tangent plane to the surface  $12+1/\sqrt{2}=x^4y-x^2y^3+y\sin z$  at the point  $(2,1,\pi/4)$ .
- 9. The point (1, -2, 4) is on the surface described by  $z = x^2y^2 + y \ln x$ . Find a vector in one of the two possible directions to go from this point to stay on the level curve z = 4.
- 10. Find all critical points for  $z = x \sin y$  and classify them as local maximum points, local minimum points, or saddle points.