

Trigonometric Identities and Integrals

The following trigonometric identities should be memorized:

The Pythagorean Identities (you get the second from the first by dividing it by $\cos^2(x)$):

$$\sin^2(x) + \cos^2(x) = 1 \qquad \tan^2(x) + 1 = \sec^2(x)$$

The double angle identities:

$$\sin(2x) = 2 \sin(x) \cos(x) \qquad \cos(2x) = \cos^2(x) - \sin^2(x)$$

The half angle identities:

$$\sin^2(x) = \frac{1}{2}(1 - \cos(2x)) \qquad \cos^2(x) = \frac{1}{2}(1 + \cos(2x))$$

Integrals you should be able to do without the table.

- Products of sine and cosine (one or more odd powers, and "simple" even powers).
- Integrate $\tan(x)$, $\tan^{-1}(x)$, $\sin^{-1}(x)$, $\ln(u)$.

The Table

The following would be provided, if needed:

$$\sin(x + y) = \sin(x) \cos(y) + \cos(x) \sin(y) \qquad \cos(x + y) = \cos(x) \cos(y) - \sin(x) \sin(y)$$

The following partial table of integrals will be provided.

- $\int \tan(u) du = \ln |\sec(u)| + C$
- $\int \cot(u) du = \ln |\sin(u)| + C$
- $\int \tan^n(u) du = \frac{1}{n-1} \tan^{n-1}(u) - \int \tan^{n-2}(u) du$
- $\int \sec(u) du = \ln |\sec(u) + \tan(u)| + C$
- $\int \csc(u) du = \ln |\csc(u) - \cot(u)| + C$
- $\int \sec^n(u) du = \frac{1}{n-1} \sec^{n-2}(u) \tan(u) + \frac{n-2}{n-1} \int \sec^{n-2}(u) du$
- $\int \sin(au) \sin(bu) du = \frac{\sin((a-b)u)}{2(a-b)} - \frac{\sin((a+b)u)}{2(a+b)}$
- $\int \sin(au) \cos(bu) du = -\frac{\cos((a-b)u)}{2(a-b)} - \frac{\cos((a+b)u)}{2(a+b)}$
- $\int \cos(au) \cos(bu) du = \frac{\sin((a-b)u)}{2(a-b)} + \frac{\sin((a+b)u)}{2(a+b)}$