

7.1

$$3) \quad \begin{array}{r} + x \cos(5x) \\ - 1 \frac{1}{5} \sin(5x) \\ + 0 - \frac{1}{25} \cos(5x) \end{array}$$

$$4) \quad \begin{array}{r} + y e^{0.2y} \\ - 1 5e^{0.2y} \\ + 0 25e^{0.2y} \end{array}$$

$$5) \quad \begin{array}{r} + t e^{-3t} \\ - 1 - \frac{1}{3} e^{-3t} \\ + 0 \frac{1}{9} e^{-3t} \end{array}$$

$$6) \quad \begin{array}{r} + x-1 \sin(\pi x) \\ - 1 - \frac{1}{\pi} \cos(\pi x) \\ + 0 \frac{1}{\pi^2} \sin(\pi x) \end{array}$$

$$7) \quad \begin{array}{r} + x^2 + 2x \cos x \\ - 2x + 2 \sin x \\ + 2 - \cos x \\ - 0 - \sin x \end{array}$$

$$8) \quad \begin{array}{r} + t^2 \sin(pt) \\ - 2t - \frac{1}{p} \cos(pt) \\ + 2 - \frac{1}{p^2} \sin(pt) \\ - 0 \frac{1}{p^3} \cos(pt) \end{array}$$

9) Use a property of logs first:

$$\ln(x^{1/3}) = \frac{1}{3} \ln(x)$$

Then: $\frac{1}{3} \int \ln x \, dx$ uses

$$\int \text{IBP:} \quad \begin{array}{r} + \ln(x) \quad 1 \\ - 1/x \quad x \end{array}$$

$$10) \quad \begin{array}{r} + \sin^{-1}(x) \quad 1 \\ - \frac{1}{\sqrt{1-x^2}} \quad x \end{array}$$

$$11) \quad \begin{array}{r} + \tan^{-1}(4t) \quad 1 \\ - \frac{1}{1+(4t)^2} \cdot 4 \quad t \end{array}$$

$$12) \quad \begin{array}{r} + \ln(p) \quad p^5 \\ - \frac{1}{p} \quad \frac{1}{6} p^6 \end{array}$$

$$13) \quad + t \sec^2(2t) \\ - 1 \quad \frac{1}{2} \tan(2t)$$

Then to integrate $\tan(2t)$,
use u, du substitution.

$$14) \quad + 5 \quad 2^5 \\ - 1 \quad \frac{1}{\ln 2} 2^5 \\ + 0 \quad \left(\frac{1}{\ln 2}\right)^2 2^5$$

$$15) \quad + (\ln(x))^2 \quad 1 \\ - 2 \ln x \cdot \frac{1}{x} \quad x$$

Then to integrate $\ln x$,
use IBP again.

16) We haven't covered
hyperbolic sine.

17) Integrate by parts twice to
get the same integral on
both sides of the equation;

$$+ \sin(3\theta) \quad e^{2\theta} \\ - 3 \cos(3\theta) \quad \frac{1}{2} e^{2\theta} \\ + -9 \cos(3\theta) \quad \frac{1}{4} e^{2\theta}$$

18) Same as 17;

$$+ e^{-\theta} \quad \cos(2\theta) \\ - -e^{-\theta} \quad \frac{1}{2} \sin(2\theta) \\ + e^{-\theta} \quad \frac{1}{4} \cos(2\theta)$$

$$19) \quad + 2^3 \quad e^z \\ - 3z^2 \quad e^z \\ + 6z \quad e^z \\ - 6 \quad e^z \\ + 0 \quad e^z$$

20) Use the identity:

$$\tan^2(x) = \sec^2(x) - 1$$

$$\text{so: } + x \quad \tan^2(x) = \sec^2 x - 1 \\ - 1 \quad \tan(x) - x$$

Then integrate $\tan(x)$
using u, du substitution.

7.1

21) Try letting $dv = \frac{1}{(1+2x)^2} dx$ and $u = xe^{2x}$

22) Try $u = (\sin^{-1}(x))^2$, $dv = dx$ (*)

23) Try $u = x$, $dv = \cos(\pi x) dx$

24) Initially, let $u = x^2 + 1$ $dv = e^{-x} dx$

25) Skip

26) Try $u = \ln y$, $dv = y^{-1/2} dy$

27) Let $u = \ln(r)$, $dv = r^3 dr$

28) Try $u = t^2$, $dv = \sin(2t) dt$

29) $u = y$, $dv = e^{-2y} dy$

30) Let $u = \tan^{-1}(\frac{1}{x})$, $dv = dx$ (then integrate $\int \frac{x dx}{1+x^2}$)

31) $u = \cos^{-1}(x)$, $dv = dx$

32) $u = \ln(x)^2$ $dv = x^{-3} dx$

33) $u = \ln(\sin(x))$ $dv = \cos(x)$

34) Let $u = r^2$, $dv = \frac{r}{\sqrt{4+r^2}}$

35) Let $u = (\ln x)^2$, $dv = x^4 dx$

~~36)~~

37) Let $y = \sqrt{x}$, $dy = \frac{1}{2\sqrt{x}} dx = \frac{1}{2y} dx$

So $\int \cos\sqrt{x} dx = \int \cos(y) (2y) dy$

$$41) \quad \left. \begin{array}{l} \text{let } y = 1+x \\ dy = dx \end{array} \right\} \int x \ln(1+x) dx = \int \underbrace{(y-1) \ln(y)} dy \\ + \ln y \quad y-1 \\ - \frac{1}{y} \quad \frac{1}{2} y^2 - y$$

Wait on this

$$+ \# \left. \begin{array}{l} (a) \text{ If } n=2, \\ (b) \int \sin^n(x) dx = \end{array} \right\} \int \sin^2(x) dx = \frac{1}{2} \cos(x) \sin(x) + \frac{1}{2} \int 1 dx \\ = x$$

$$63) \quad \text{Vol} = \int_{-1}^0 2\pi (1-x) e^{-x} dx \quad \text{etc}$$

$$\star \underline{68)} \quad \begin{array}{r} + f(x) \quad g''(x) \\ - f'(x) \quad g'(x) \\ + f''(x) \quad g(x) \end{array}$$

$$\Rightarrow f(x) g'(x) \Big|_0^a - f'(x) g(x) \Big|_0^a + \int_0^a f''(x) g(x) dx$$

76) Just do (a)