## Practice with Algebra and Integrals

Here are some practice problems of the type you might find useful. For integration by parts, try to use the table version- it can make the problem go much faster!;

## **Practice with Partial Fractions**

1. 
$$\int \frac{2x^2 - x + 4}{x^3 + 4x} dx$$
  
2.  $\int \frac{1}{y(2-y)} dy$   
3.  $\int \frac{x-1}{x^2+1} dx$   
4.  $\int \frac{dx}{x^4 - x^2}$ 

## Practice with Integration by Parts

1. 
$$\int e^{2\theta} \sin(3\theta) d\theta$$
  
2. 
$$\int t^2 \cos(3t) dt$$
  
3. 
$$\int x^3 e^x dx$$
  
4. 
$$\int \tan^{-1}(x) dx$$

## Algebra practice with logs and exponentials

1. Write each expression in logarithmic form

(a) 
$$a^b = c$$
 (b)  $100^{1/2} = 10$  (c)  $(3/4)^{-1} = 4/3$  (d)  $2^5 = 32$ 

2. Write each expression in exponential form

(a) 
$$\log_a(b) = c$$
 (b)  $\log_{10}(0.001) = -3$  (c)  $\log_2(\sqrt{32}) = 5/2$ 

3. Solve each equation:

(a) 
$$10^{2r-3} = 17$$
  
(b)  $\log_2(y+3) = 5$   
(c)  $(1/2)^{3k+1} = 3$   
(d)  $\ln(6x) - \ln(x+1) = \ln(4)$ 

4. Use properties of logs to write each as a sum, difference or product of logarithms:

(a) 
$$\log_3\left(\frac{mn}{5r}\right)$$
 (b)  $\log_2\left(\frac{\sqrt{7}}{15}\right)$  (c)  $\log_5\left(x^2y^4\sqrt[5]{m^3p}\right)$  (d)  $\log_7(7k+5r^2)$ 

5. Simplify:  $e^{a \ln(b)}$