Extra Practice: Section 2.5

Given the differential equation, identify if each is *linear* (L), *separable* (S), *autonomous* (A), *Bernoulli* (B), and/or *homogeneous* (H). Recall that any given DE may have multiple labels.

(a)
$$\frac{dy}{dx} = \frac{x^3 - 2y}{x}$$

(b)
$$\frac{dy}{dx} = \frac{x + y}{x - y}$$

(c)
$$(e^x + 1)\frac{dy}{dx} = y - ye^x$$

(d)
$$\frac{dy}{dt} = \cos(y)$$

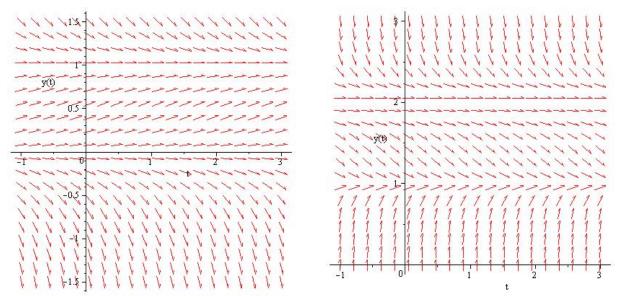
(e)
$$\frac{dy}{dt} = \cos(t)$$

(f)
$$t^2y' + 2ty - y^3 = 0$$

2. Suppose we are given the differential equation:

$$y' = \sin(y)$$

- (a) True or False: The solution may be periodic.
- (b) What happens to the solution corresponding to y(0) = 1? How about y(0) = 100? (HINT: Do not solve!)
- 3. Below are two direction fields (in the (t, y) plane). Find an autonomous differential equation, y' = F(y), that is consistent with each one. Proceed by first sketching a consistent function for each direction field in the (y, y') plane.



- 4. Let y' = y(y 1).
 - (a) Give the general solution.
 - (b) Plot the appropriate function in the (y, y') plane, and classify the equilibria as to stability.
 - (c) Without going to the solution y(t), find intervals on which y(t) will be concave up and concave down.
- 5. For each fraction, write down what the partial fraction expansion would be (but do not solve for the constants!):

(a)
$$\frac{x^2 - 3x + 1}{x(x - 1)(x - 2)}$$

(b)
$$\frac{3x - 1}{x^2(x - 1)}$$

(c)
$$\frac{3x - 1}{(x^2 + 1)(x^2 + 4)^2}$$