## Homework Addendum for 4.1-4.3

- 1. Show that the intersection of two convex sets is convex.
- 2. If we define a *hyperplane* as the set of vectors  $\mathbf{x}$  so that  $\mathbf{c}^T \mathbf{x} b = 0$  for some constant vector  $\mathbf{c}$  and scalar b, then show that a hyperplane is convex.
- 3. Show that the convex hull of a given set of k vectors is convex.
- 4. Find a **convex combination** of the vertices of the polygonal region below for the point (1, 2). You may do this all in two dimensions.

5. Consider the feasible set:

$$\begin{array}{rrrr} 2x+&y\geq 4\\ x+&2y\geq 6\\ -x&+2y\geq 2\\ x,&y\geq 0 \end{array}$$

- (a) Write the feasible set in standard form.
- (b) Find a direction of unboundedness, **d**.
- (c) Write the point corresponding to (2, 4) using Theorem 2, page 135. Be sure to pay attention to the appropriate dimensions!