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> # Example 3: Preemptive programming
with(LinearAlgebra):
interface(rtablesize=11);
                                10
(1)
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> # Vars: x1 x2 e1 e2 e3 s1 s2 s3 (and rhs)
A:=<<0,0,0,7,10,5,100>|<0,0,0,3,5,4,60>|<0,0,0,-1,0,0,0>|<0,0,0,
0,-1,0,0>|<0,0,0,0,0,-1,0>|<P1,0,0,1,0,0,0>|<0,P2,0,0,1,0,0>|<0,
0,P3,0,0,1,0>|<0,0,0,0,0,0,1>|<0,0,0,40,60,35,600>>;
A:=
(2)
```

$$\begin{bmatrix}
0 & 0 & 0 & 0 & 0 & P1 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & P2 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 0 & 0 & P3 & 0 & 0 \\
7 & 3 & -1 & 0 & 0 & 1 & 0 & 0 & 0 & 40 \\
10 & 5 & 0 & -1 & 0 & 0 & 1 & 0 & 0 & 60 \\
5 & 4 & 0 & 0 & -1 & 0 & 0 & 1 & 0 & 35 \\
100 & 60 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 600
\end{bmatrix}$$

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> #
A2:=RowOperation(A,[1,4],-P1):
A3:=RowOperation(A2,[2,5],-P2):
A4:=RowOperation(A3,[3,6],-P3);
A4:=
(3)
```

$$\begin{bmatrix}
-7 P1 & -3 P1 & P1 & 0 & 0 & 0 & 0 & 0 & 0 & -40 P1 \\
-10 P2 & -5 P2 & 0 & P2 & 0 & 0 & 0 & 0 & 0 & -60 P2 \\
-5 P3 & -4 P3 & 0 & 0 & P3 & 0 & 0 & 0 & 0 & -35 P3 \\
7 & 3 & -1 & 0 & 0 & 1 & 0 & 0 & 0 & 40 \\
10 & 5 & 0 & -1 & 0 & 0 & 1 & 0 & 0 & 60 \\
5 & 4 & 0 & 0 & -1 & 0 & 0 & 1 & 0 & 35 \\
100 & 60 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 600
\end{bmatrix}$$

```
> # Work through Priority 1 first (Row 1): Pivot in Column 1
evalf([40/7,60/10,35/5,600/100]);
[5.714285714, 6., 7., 6.]
(4)
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> #
A5:=RowOperation(A4,4,1/7):
A6:=RowOperation(A5,[1,4],7*P1):
A7:=RowOperation(A6,[2,4],10*P2):
A8:=RowOperation(A7,[3,4],5*P3):
A9:=RowOperation(A8,[5,4],-10):
A10:=RowOperation(A9,[6,4],-5):
A11:=RowOperation(A10,[7,4],-100);
```

$$A11 := \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & P1 & 0 & 0 & 0 & 0 \\ 0 & -\frac{5}{7} P2 & -\frac{10}{7} P2 & P2 & 0 & \frac{10}{7} P2 & 0 & 0 & 0 & -\frac{20}{7} P2 \\ 0 & -\frac{13}{7} P3 & -\frac{5}{7} P3 & 0 & P3 & \frac{5}{7} P3 & 0 & 0 & 0 & -\frac{45}{7} P3 \\ 1 & \frac{3}{7} & -\frac{1}{7} & 0 & 0 & \frac{1}{7} & 0 & 0 & 0 & \frac{40}{7} \\ 0 & \frac{5}{7} & \frac{10}{7} & -1 & 0 & -\frac{10}{7} & 1 & 0 & 0 & \frac{20}{7} \\ 0 & \frac{13}{7} & \frac{5}{7} & 0 & -1 & -\frac{5}{7} & 0 & 1 & 0 & \frac{45}{7} \\ 0 & \frac{120}{7} & \frac{100}{7} & 0 & 0 & -\frac{100}{7} & 0 & 0 & 1 & \frac{200}{7} \end{bmatrix} \quad (5)$$

> # Priority 1 finished. Move to Priority 2 (Column 3, Row 5 (tie))
 evalf([(20/7)/(10/7), (45/7)/(5/7), (200/7)/(100/7)]);
 [2., 9., 2.]

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> #
 A12:=RowOperation(A11,5,7/10):
 A13:=RowOperation(A12,[2,5],(10/7)*P2):
 A14:=RowOperation(A13,[3,5],(5/7)*P3):
 A15:=RowOperation(A14,[4,5],1/7):
 A16:=RowOperation(A15,[6,5],-5/7):
 A17:=RowOperation(A16,[7,5],-100/7);

$$A17 := \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & P1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & P2 & 0 & 0 & 0 \\ 0 & -\frac{3}{2} P3 & 0 & -\frac{1}{2} P3 & P3 & 0 & \frac{1}{2} P3 & 0 & 0 & -5 P3 \\ 1 & \frac{1}{2} & 0 & -\frac{1}{10} & 0 & 0 & \frac{1}{10} & 0 & 0 & 6 \\ 0 & \frac{1}{2} & 1 & -\frac{7}{10} & 0 & -1 & \frac{7}{10} & 0 & 0 & 2 \\ 0 & \frac{3}{2} & 0 & \frac{1}{2} & -1 & 0 & -\frac{1}{2} & 1 & 0 & 5 \\ 0 & 10 & 0 & 10 & 0 & 0 & -10 & 0 & 1 & 0 \end{bmatrix} \quad (7)$$

> # Priority 2 finished. Move to Priority 3, Pivot in Column 2 (last row)

> #

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A18:=RowOperation(A17,7,1/10):
A19:=RowOperation(A18,[3,7],(3/2)*P3 ):
A20:=RowOperation(A19,[4,7],-1/2):
A21:=RowOperation(A20,[5,7],-1/2):
A22:=RowOperation(A21,[6,7],-3/2);

```

$$A22:= \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & P1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & P2 & 0 & 0 & 0 \\ 0 & 0 & 0 & P3 & P3 & 0 & -P3 & 0 & \frac{3}{20} P3 & -5 P3 \\ 1 & 0 & 0 & -\frac{3}{5} & 0 & 0 & \frac{3}{5} & 0 & -\frac{1}{20} & 6 \\ 0 & 0 & 1 & -\frac{6}{5} & 0 & -1 & \frac{6}{5} & 0 & -\frac{1}{20} & 2 \\ 0 & 0 & 0 & -1 & -1 & 0 & 1 & 1 & -\frac{3}{20} & 5 \\ 0 & 1 & 0 & 1 & 0 & 0 & -1 & 0 & \frac{1}{10} & 0 \end{bmatrix}$$

(8)

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> # Done...
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